

$$\varphi = \text{rad}(\text{lon})$$

$$\theta = \text{rad}(\text{lat})$$

$$\vec{\mathbf{v}} = \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} r \cos(\theta) \cos(\varphi) \\ r \cos(\theta) \sin(\varphi) \\ r \sin(\theta) \end{bmatrix}$$

$$B = \{\vec{v}_1, \dots, \vec{v}_m\}$$

$$B = \left\{ \begin{bmatrix} v_{1_1} \\ \vdots \\ v_{1_n} \end{bmatrix}, \dots, \begin{bmatrix} v_{m_1} \\ \vdots \\ v_{m_n} \end{bmatrix} \right\}$$

$$\overrightarrow{b_{avg}} = \begin{bmatrix} \text{avg}(v_{1_1}, \dots, v_{m_1}) \\ \vdots \\ \text{avg}(v_{1_n}, \dots, v_{m_n}) \end{bmatrix}$$

$$\triangle UVW = \left\{ \begin{bmatrix} x_u \\ y_u \end{bmatrix}, \begin{bmatrix} x_v \\ y_v \end{bmatrix}, \begin{bmatrix} x_w \\ y_w \end{bmatrix} \right\}$$

$$x_p = u\,x_u + v\,x_v + w\,x_w$$

$$y_p = u\,y_u + v\,y_v + w\,y_w$$

$$\vec{p} = \begin{bmatrix} x_p \\ y_p \end{bmatrix}$$

$$\begin{aligned} u &= \frac{(y_v - y_w)(x_p - x_w) + (x_w - x_v)(y_p - y_w)}{(y_v - y_w)(x_u - x_w) + (x_w - x_v)(y_u - y_w)} \\ v &= \frac{(y_w - y_u)(x_p - x_w) + (x_u - x_w)(y_p - y_w)}{(y_v - y_w)(x_u - x_w) + (x_w - x_v)(y_u - y_w)} \\ w &= 1 - u - v \end{aligned}$$

$$V = \{\vec{v}_1, \dots, \vec{v}_i, \dots, \vec{v}_m\}$$

$$= \left\{ \begin{bmatrix} v_{1_1} \\ \vdots \\ v_{1_j} \\ \vdots \\ v_{1_n} \end{bmatrix}, \dots, \begin{bmatrix} v_{i_1} \\ \vdots \\ v_{i_j} \\ \vdots \\ v_{i_n} \end{bmatrix}, \dots, \begin{bmatrix} v_{m_1} \\ \vdots \\ v_{m_j} \\ \vdots \\ v_{m_n} \end{bmatrix} \right\}$$

$$\omega_i = \text{mort}(\vec{v}_i)$$

$$= \text{mort}(v_{i_1}, \dots, v_{i_j}, \dots, v_{i_n})$$

$$\text{home}_\omega(V) = \{\omega_1, \dots, \omega_i, \dots, \omega_m\}$$